CLAIMS

We claim:

A method for editing a geometrical model with a level set modeling surface
 editor operator, comprising:

performing a level set surface editing operation on a level set model, wherein said operation is defined by a level set surface editing operator.

2. The method of claim 1 further comprises:

converting an input model into said level set model for said step of performing a level set surface editing operation;

rendering said level set model after said step of performing a level set surface editing operation.

- The method of claim 2 wherein said converting step converts said input model from a geometric to a volumetric model by using scan conversion.
 - 4. The method of claim 2 wherein said converting step converts said input model with by using distance calculations.

5. The method of claim 2 wherein said converting step converts said input model with by using Sethian's Fast Marching Method.

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- 6. The method of claim 1 wherein said level set model is represented in a narrow-band distance volume.
- 7. The method of claim 1 wherein said performing a level set surface editing
- 5 operator is defined as a speed function, said function comprising:
 - a regional constraint function component;
 - a filter function component;
 - a surface properties defining function component.
- 10 8. The method of claim 7 wherein said speed function is

$$F(x, n, \phi) = D_a(d)C(\gamma)G(\gamma)$$
, wherein

- $D_q(d)$ is said regional constraint function component,
- $C(\gamma)$ is said filter function component, and
- $G(\gamma)$ is said surface properties defining function component.
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- 9. The method of claim 8 wherein said $D_q(d)$ is further defined as having q be a geometric primitive such as a point, a line-segment, or surface and d be the distance from the level set surface of said level set surface model to q.
- 20 10. The method of claim 8 wherein said γ is a geometric property of the level set surface of said level set surface model, wherein γ is any order property of ϕ .

- 11. The method of claim 10 wherein γ represents distance, which is the zero-th order property of ϕ .
- 12. The method of claim 10 wherein γ represents normal vector to said level set surface, which is the first order property of ϕ .
 - 13. The method of claim 10 wherein γ represents curvature of said level set surface, which is the second order property of ϕ .
- 10 14. The method of claim 8 wherein said regional constraint component defines a region-of-influence.
 - 15. The method of claim 14 wherein said region-of-influence is defined by a distance calculation to a geometric primitive such as a point set, a line segment, or a surface.
 - 16. The method of claim 15 wherein said region-of-influence is defined by a distance to an intersection curve point set.
 - 17. The method of claim 15 wherein said region-of-influence is a super-ellipsoid.
 - 18. The method of claim 8 wherein said filter function component is a filter of local geometric surface properties, wherein user can control the behavior of said level set surface editing operator based on a function of a local geometric surface property.

- 19. The method of claim 8 wherein said surface properties defining function component defines the behavior of said level set surface editing operator.
- The method of claim 1 wherein said level surface editing operator is a CSGintersection operator.
 - 21. The method of claim 1 wherein said level surface editing operator is a CSG difference operator.
- 10 22. The method of claim 1 wherein said level surface editing operator is a CSG union operator.
 - 23. The method of claim 7 wherein said level surface editing operator is a blending operator, wherein blending is constrained by a region-of-influence.

- 24. The method of claim 23 wherein said region-of-influence is based on the distance to an intersection curve shared by both input surfaces.
- 25. The method of claim 23 wherein said intersection curve is represented by a 20 point set.
 - 26. The method of claim 23 wherein said blending operator is defined by the function $F_{blend}(x, n, \phi) = \alpha D_a(d)C(K)K$, wherein

 α is a user-defined positive scalar that controls the rate of the level set calculation; $D_q(d)$ is said region-of-influence component with d being the shortest distance from the level set surface to said intersection curve point set;

K is a curvature term; and

- C(K) is a filtering function that defines the geometric properties of said blending operator.
- The method of claim 23 wherein said blending operator calculates a closest point in a set by using the approximate nearest neighbor search algorithm of Mount and
 Arya.
 - 28. The method of claim 27 wherein said blending operator calculates a closest point in a set by storing a point set in a K-D tree, wherein points in said point set is are uniform distributed.

- 29. The method of claim 27 wherein said blending operator calculates a closest point in a set by storing a point set in the balanced box decomposition (BBD) tree, wherein points in said point set is are clustered.
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- 30. The method of claim 7 wherein said level surface editing operator is a smoothing operator, wherein a surface is smoothed by applying motions in a direction that reduces local curvature.

- 31. The method of claim 30 wherein said smoothing operator is constrained to move outward relative to said surface to smooth said surface by adding material to said surface.
- 5 32. The method of claim 30 wherein said smoothing operator is constrained to move inward relative to said surface to smooth said surface by removing material to said surface.
- 33. The method of claim 30 wherein said smoothing operator is converted into a sharpening operator by changing the sign of a scalar term and using said filter function to truncate said speed-function to zero for high values of the curvature.
 - 34. The method of claim 30 wherein said smoothing operator is defined by the function $F_{smooth}(x, n, \phi) = \alpha D_s(d) C(K) K$, wherein
- lpha is a user-defined positive scalar that controls the rate of the level set calculation; $D_s(d)$ ensures that said function smoothly goes to zero near the boundary of the region-of-influence;

K is a curvature term; and

C(K) is a filtering function that defines the geometric properties of said smoothing operator.

- 35. The method of claim 34 wherein said region-of-influence of said $D_s(d)$ is defined said by a distance calculation to a geometric primitive such as a point set, a line segment, or a surface.
- 5 36. The method of claim 35 wherein said smoothing operator calculates a closest point in a set by using the approximate nearest neighbor search algorithm of Mount and Arya.
- 37. The method of claim 36 wherein said smoothing operator calculates a closest point in a set by storing a point set in a K-D tree, wherein points in said point set is are uniform distributed.
 - 38. The method of claim 36 wherein said smoothing operator calculates a closest point in a set by storing a point set in the balanced box decomposition (BBD) tree, wherein points in said point set is are clustered.
 - 39. [new] The method of claim 35 wherein said region-of-influence is a superellipsoid.
- 20 40. The method of claim 7 wherein said level surface editing operator is a point set attraction/repulsion operator.

- 41. The method of claim 40 wherein said point set attraction/repulsion operator calculates a closest point in a set by using the approximate nearest neighbor search algorithm of Mount and Arya
- The method of claim 41 wherein said point set attraction/repulsion operator calculates a closest point in a set by storing a point set in a K-D tree, wherein points in said point set is are uniform distributed.
- 43. The method of claim 41 wherein said point set attraction/repulsion operator

 10 calculates a closest point in a set by storing a point set in the balanced box decomposition

 (BBD) tree, wherein points in said point set is are clustered.
 - 44. The method of claim 40 wherein said point set attraction/repulsion operator is used to emboss a surface.
 - 45. The method of claim 1 wherein said level surface editing operator is a morphological editing operator.
 - 46. The method of claim 2 wherein said rendering uses a volume rendering.
 - 47. The method of claim 2 wherein said rendering uses Incremental Marching Cubes mesh extraction, which optimizes the mesh extraction by limiting the region which needs to be processed.

- 48. The method of claim 2 wherein said input model is a polygon mesh.
- 49. The method of claim 48 wherein said polygon mesh is scan converted into a level set model by computing a distance volume, wherein said computing calculates the closest point on and shortest singed distance to said mesh by solving the Eikonal equation $|\nabla \phi| = 1$.
 - 50. The method of claim 49 wherein said computing a distance volume uses the CPT (closest point) algorithm of Mauch.
 - 51. The method of claim 2 wherein said input model is a Constructive Solid Geometry (CSG) model.
 - 52. The method of claim 2 wherein said input model is an implicit model.
 - 53. The method of claim 2 wherein said input model is a scanned volume.
 - 54. The method of claim 8 further comprises:

resetting the volumetric representation of said level model after said step of 20 performing a level set surface editing operation to ensure that ϕ is approximately equal to the shortest distance to the zero level set in the narrow band.

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55. The method of claim 7 wherein level set computations associated with solving said speed function are regionally constrained to a sub-volume defined by the bounding-box of a region-of-influence primitive.